State-aware anomaly detection for massive sensor data in Internet of Things

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ABSTRACT

With the escalating prevalence of Internet of Things (IoTs) in critical infrastructure, the requirement for efficient and effective anomaly detection solution becomes increasingly important. Unfortunately, most prior research works have largely overlooked to adapt detection criteria for different operational states, thereby rendering them inadequate when confronted with diverse and complex work states of IoTs. In this study, we address the challenges of IoT anomaly detection across various work states by introducing a novel model called Hybrid State Encoder-Decoder (HSED). HSED employs a two-step approach, beginning with identification and construction of a hybrid state for Key Performance Indicator (KPI) sensors based on their state attributes, followed by the detection of abnormal or failure events utilizing high-dimensional sensor data. Through the evaluation on real-world datasets, we demonstrate the superiority of HSED over state-of-the-art anomaly detection models. HSED can significantly enhance the efficiency, adaptability and reliability of IoTs and avoid potential risks of economic losses by IoT failures.

KEYWORDS

Anomaly detection, Internet of Things, State-aware monitoring

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With the growth of cyber technologies and communication networks, Internet of Things (IoTs) have witnessed a remarkable surge in critical infrastructure domains, such as transportation networks, energy systems, water and gas distribution networks, as well as unmanned factories. The salient feature of IoTs lies in the ability to establish a tight connection between computational and physical components. By seamlessly integrating physical and cyber elements, IoTs can execute intricate real-time tasks by acquiring data from sensors, conducting data analysis, and initiating actions based on the obtained insights. Nevertheless, as the scale and complexity of IoTs continue to expand at a rapid pace, the consequences of system failures or security breaches can be severe, even posing

Therefore, it is necessary to develop data-centric anomaly detection solutions to automatically monitoring the operation of IoTs. The solution should be able to analyze large volumes of data in realtime, facilitate early detections of anomalies and prompt remedial measures. A major challenge to implement such a solution is on building the system profile for different work states. Most IoTs have multiple work states (i.e., operational modes). The normal dynamics exhibited by Key Performance Indicator (KPI) sensors may vary across different work states. Unfortunately, most existing anomaly detection methods cannot adapt their models in accordance with the work state. Consequently, they may report lots of false alerts when IoTs change the work states in a normal manner, or miss the real anomalies while testing with a wrong profile model.

Furthermore, the anomaly detection across multiple work states presents a series of challenges: First, the dynamics of work states are intricately linked to system operations or transitions. Due to a lack of domain expertise, most users cannot provide accurate and detailed information of the work states. Instead, they would like the monitoring system to learn the work states and provide them as output. Second, the data acquired from IoT sensors typically exhibits high dimensionality and is prone to noise. It is difficult to direct extract meaningful information from such data without a clear indicator. Last, the system behavior and associated dynamics can vary significantly among different states. Such distances among normal states may be magnitude larger than the difference of normal/abnormal behaviors.

1 INTRODUCTION

life-threatening risks.

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In this study, we address the above challenges of IoT anomaly detection and propose a novel framework called Hybrid State Encoder-Decoder (HSED). The major contributions are listed as follows:

- HSED employs state encoders model to recover multiple hidden states for the IoT. The system extracts embedding features from individual state and constructs a hybrid model to address dynamic work states.
- HSED reconstructs the sensor signals based on the hybrid hidden state of IoT. The system then conducts anomaly detection by comparing the reconstructed signals with original ones.
- HSED is deployed and evaluated on real world dataset. HSED achieves higher accuracy in anomaly detection tasks comparing to other state-of-the-art methods.

2 RELATED WORK

In recent years, there has been a notable surge of interest on applying deep learning-based approaches for anomaly detection in IoT data [8]. Most methods focus on anomaly detection by reconstructing the sensor data with deep models. Recurrent Neural Networks (RNNs) have gained widespread adoption for capturing temporal dependencies in IoTs [4, 13], and auto-encoders are commonly employed to model correlations among diverse sensors [1, 2].

Recurrent Variational Auto-Encoder (VAE) architectures have been used to construct non-linear state space models [6] and facilitate the learning of disentangled representations [3]. RNN-based deep state space models have been proposed Rangapuram et al. [10], Salinas et al. [11] to accomplish probabilistic sensor data forecasting. However, the majority of these approaches are limited to constructing a single model and are not well-suited for addressing the diverse work states in IoT applications. Moreover, these methods require the users to input prior domain-specific knowledge. Their applicability is also restricted and confined to some specific domains, such as power management.

One of the seminal works in contextual anomaly detection is Conditional Anomaly Detection (CAD) [12]. This method requires users to partition features into contextual and behavioral categories. The method uses Gaussian Mixture Models (GMM) to fit the distributions of the contextual and behavioral feature spaces and learns dependencies between them. Another method, the Robust Contextual Outlier Detection (ROCOD) method [7], uses both local and global models to describe the relationships between contextual and behavioral features. The main problem of above methods is on the assumption. They rely on the assumption that features adhere to specific statistical distributions, such as GMM. However, this assumption may prove to be too restrictive in real-world scenarios. It can potentially hinder the accuracy of the results obtained from these methods.

3 PROBLEM DEFINITION

Let $X = \{X_1, ..., X_n\}$ be the historical data-set, which consists of n different sensor data. Each sensor data $X_t \in \mathbb{R}^{d \times T}$ is a multivariate time series with length T and for each time step $1 \le t \le T$, $X_{i,t} = [C_{i,t}, S_{i,t}] \in \mathbb{R}^{d_1+d_2}$ is the corresponding multi-variate vector

Algorithm 1 HSED

Paguire: Number of different states m
Require. Number of unferent states <i>m</i>
 Extracting the feature embedding by
$\operatorname{Enc}(\cdot), \{\operatorname{Center}_j\}_{j=1}^m \leftarrow \operatorname{Cond-Embedding}(\mathcal{C})$
2: Set the similarity matrix by
$S(\mathbf{C}_i, \operatorname{Center}_j) = \ \operatorname{Enc}(\mathbf{C}_i) - \operatorname{Center}_j\ _2$
3: Set the hybrid hidden-states as
$\mathbf{P}_{i,j} \sim (1 + S(\mathbf{C}_i, \operatorname{Center}_j)/\alpha)^{-(1+\alpha)/2}$
4: for each main state C_i and KPI attributes S_i do
5: Extracting the embedding for KPI attributes S_i within state
C_j
Embedding _{<i>i</i>} (·) \leftarrow Sensor-Embedding (S_i , $P_{i,j}$)
6: end for
7: For each sequence S_i , combining the embedding and recovering
the original sequence

 $S'_i, S'_{i,b} \leftarrow \text{Rec}(\{\text{Embedding}_i(S_i), P_{i,j}\}_{i=1}^m)$

with dimension $d = d_1 + d_2$. Here, $S_{i,t} \in \mathbb{R}^{d_2}$ is the data collected from KPI sensors.

Note that, the value of KPI sensors can vary significantly across different work states. To incorporate these information, we introduce contextual variables $C_{i,t} \in \mathbb{R}^{d_1}$ to denote the state attributes, which indicates the dynamic of the work state.

In general, anomaly detection can be divided into two categories: point anomalies and contextual anomalies. Point anomalies refer to data points that deviate significantly from the expected behavior observed throughout the entire trajectory. On the other hand, contextual anomalies pertain to data points that exhibit significant deviations from the expected behavior within a particular context or environment. The identification of contextual anomalies necessitates considering the specific environment or context in which the data point is observed. Contextual anomalies are more difficult to detect than point anomalies, and we focus on the detection of contextual anomalies in this study.

Problem Definition (Anomaly Detection): Let $\{S_1, ..., S_n\}$ be the historical dataset of normal operation, and $\{C_1, ..., C_n\}$ be the state information, the task is to learn a model \mathcal{M} , such that when new streaming data X comes in, the model \mathcal{M} can detect whether X is abnormal or not.

4 THE HSED FRAMEWORK

In this section, we propose a noval framework called Hybrid State Encoder-Decoder (HSED) to detect the anomalies in sensor data of IoTs. The overall system structure is shown in Figure 1. And the main steps are illustrated in Algorithm 1.

4.1 Distinguish Hidden States

Since the dynamic of KPI sensor *S* highly relied on the hidden state, it becomes imperative to first uncover the hidden state before proceeding with anomaly detection. Hence, in HSED algorithm (Line 1), we employ an auto-encoder-based deep temporal clustering mechanism **Cond-Embedding** [5] to distinguish the hidden state from the state attributes $C = \{C_1, .., C_n\}$, where each clustering Center *i* corresponding to a different state. The whole process is

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Figure 1: The overall framework for the HSED and details for each steps can be found in Section 4.1 to 4.5.

shown as Algorithm 2: Given the input sequence $C_i \in \mathbb{R}^{d_1 \times T}$, we use sequential GRU-cells as encoder to extract the time-series information from both the forward sequence C_i and the corresponding inverse sequence $C_{i,b}$. After receiving the feature embedding matrices $\mathbf{H}_{f}, \mathbf{H}_{b} \in \mathbb{R}^{T \times l}$, we introduce the attention mechanism (Lines 4 to 6) to aggregate the feature across different timestamps. Based on the final embedding feature $Enc(C_i)$, we reconstruct the original sequence with a GRU-based decoder (Line 7) and also perform K-Means algorithm with the embedding feature to generate different clusters (Line 8). Based on the reconstruction error and clustering error, the training loss of algorithm 2 consists of the following three parts:

$$Loss = \alpha \cdot \underbrace{\sum_{i=1}^{n} \|C_i - C'_i\|_2^2}_{Auto-encoder forward loss} + \alpha \cdot \underbrace{\sum_{i=1}^{n} \|C_{i,b} - C'_{i,b}\|_2^2}_{K-mean loss}$$

where $Center(Enc(C_i))$ correspond to the closest center for the feature embedding $Enc(C_i)$. In Algorithm 2, we aim to minimize the training loss and update the parameters θ_f , θ_b with gradient descent.

4.2 **Hybrid State Construction**

Now HSED has distinguished the hidden states Center_i. However, time series X_i may not fall into each state, the smoothly dynamic of the hidden state and the existence of some intermediate state makes it more difficulty to detect the abnormal events. To capture the smoothly switching of hidden states and corresponding intermediate states, we develop a similarity-based mechanism to discover the hybrid states and decomposes each time series X_i to the hybrid of multiple basic hidden states. More specifically, for each time series X_i , we focus on the state attributes C_i and first extract the feature embedding $Enc(C_i)$ from Algorithm 2. Then each state attributes C_i and the hidden state Center *i*, we compute the similarity,

Algorithm 2 Cond-Embedding

- Require: Number of different states *m*, Forward and backward parameters θ_f, θ_b
- 1: **Input**: state attributes $C_i \in \mathbb{R}^{d_1 \times T} = [\mathbf{x}_1, ..., \mathbf{x}_T]$
- 2: Create the inverse sequence $C_{i,b} = [\mathbf{x}_T, ..., \mathbf{x}_1]$
- 3: Let $\mathbf{H}_{f} \leftarrow \mathbf{GRU}_{\theta_{f}}(\mathbf{C}_{i}) = [\mathbf{h}_{1}, ..., \mathbf{h}_{T}], \mathbf{H}_{b} \leftarrow \mathbf{GRU}_{\theta_{b}}(\mathbf{C}_{i,b}) =$ $[\mathbf{h}_{1,b}, .., \mathbf{h}_{T,b}]$
- 4: $\mathbf{u}_f = \tanh(H_f \cdot \mathbf{W}_f + \boldsymbol{b}_f), \mathbf{u}_b = \tanh(H_b \cdot \mathbf{W}_b + \boldsymbol{b}_b)$
- 5: $\mathbf{w}_{f,t} = \text{Soft-Max}(\mathbf{u}_{f} \circ \mathbf{h}_{t}), \mathbf{w}_{b,t} = \text{Soft-Max}(\mathbf{u}_{b} \circ \mathbf{h}_{t,b})$ 6: $\mathbf{h}_{f}^{\text{attention}} = \sum_{t=1}^{T} \mathbf{w}_{f,t} \mathbf{h}_{t}, \mathbf{h}_{b}^{\text{attention}} = \sum_{t=1}^{T} \mathbf{w}_{b,t} \mathbf{h}_{t,b}$ 7: Set embedding feature $\text{Enc}(\mathbf{C}_{i}) = \mathbf{h}_{f}^{\text{attention}} + \mathbf{h}_{b}^{\text{attention}}$
- 8: Reconstruct the sequences $C'_i \leftarrow GRU_{\theta_f}(Enc(C_i)), C'_{i,b} \leftarrow$ $GRU_{\theta_h}(Enc(C_i))$
- 9: Perform K-mean algorithm for the embedding feature $Enc(C_i)$ and return the centers: {Center_j}^{*m*}_{*i*=1}

which is denote by the euclidean distance between $Enc(C_i)$ and Center_{*i*}: $S(C_i, Center_i) = ||Enc(C_i) - Center_i||_2$ (Line 2). At last, we construct the hybrid state with the Student's t distribution and generate the weight matrix $\mathbf{P}_{i,j} \sim (1 + S(\mathbf{C}_i, \operatorname{Center}_i)/\alpha)^{-(1+\alpha)/2}$ (Line 3), where $w_{i,j}$ represents the probability to assign state series C_i to main state Center_i. With the help of this weighted matrix P, the hidden state for series Xi can be decomposed as a hybrid of main states.

4.3 Extract Embedding Features

After constructing the hybrid states, HSED employs a LSTM-based encoder to extract the features from the KPI sensors S_i . Since the sensor data of different states can be totally different, HSED needs to collect the features of various information such as period or magnitude across multiple states. Therefore, HSED constructs individual encoders and decoders for each main state Center *j* separately and the detailed algorithm is shown in Algorithm 3. Specifically, the encoder consists two different LSTM-based units to process the KPI sensor data: the first one is used to aggregate the time-series Al4Cyber, August 7, 2023, Long Beach, California, XXXX

Algorithm 3 Sensor-Embedding

Require: Number of different states *m*, Forward and backward parameters $\theta_{f,j}, \theta_{b,j}$

- 1: **Input**: KPI attributes $S_i \in \mathbb{R}^{d_2 \times T} = [\mathbf{y}_1, .., \mathbf{y}_T]$, Hybrid-state matrix $\mathbf{P}_{i,i}$
- 2: Create the inverse sequence $S_{i,b} = [\mathbf{y}_T, .., \mathbf{y}_1]$
- 3: Let $\mathbf{h}_{f} \leftarrow \mathbf{LSTM}_{\theta_{f,i}}(S_{i}), \mathbf{h}_{b} \leftarrow \mathbf{LSTM}_{\theta_{b,i}}(S_{i,b})$
- 4: Set embedding feature $\text{Embedding}_j(S_i) = \text{Concatenate}(\mathbf{h}_f, \mathbf{h}_b)$
- 5: Reconstruct the sequences $S'_i \leftarrow \text{LSTM}_{\theta_{f,j}}(\text{Embedding}_j(S_i))$, $S'_{i,b} \leftarrow \text{LSTM}_{\theta_{b,j}}(\text{Embedding}_j(S))$

Algorithm 4 Rec

- **Require:** Number of different states *m*, Forward and backward parameters θ_f, θ_b
- Input: Embedding feature {Embedding_j(S_i)}^m_{j=1}, Hybrid-state matrix P_{i,j}
- 2: Set embedding feature $\text{Embedding}(S_i) = \text{Concatenate}(\mathbf{P}_{i,j} \cdot \text{Embedding}_i(S_i))$
- 3: Reconstruct the sequences::

$$S'_i \leftarrow \text{LSTM}_{\theta_f}(\text{Embedding}(S_i)),$$

$$S'_{i,b} \leftarrow \text{LSTM}_{\theta_b}(\text{Embedding}(S))$$

information from the forward sequence and the other focused on the backward sequence (Line 3). After concatenating the output of two different units \mathbf{h}_f , \mathbf{h}_b (Line 4), HSED obtains the encoding feature Embedding_{*j*}(S_i) and feed it into the decoder to reconstruct the original sequence (Line 5). Finally, since each time series S_i is not purely belong to one main state Center_{*j*}, the reconstruction error for each main state Center_{*j*} is also weighted by the hybrid-state matrix $\mathbf{P}_{i,j}$ as following:

Loss_j =
$$\sum_{i=1}^{n} \mathbf{P}_{i,j} \| \mathbf{S}_i - \mathbf{S}'_i \|_2^2 + \sum_{i=1}^{n} \mathbf{P}_{i,j} \| \mathbf{S}_i, b - \mathbf{S}'_{i,b} \|_2^2$$

Hybrid Auto-encoder forward loss Hybrid Auto-encoder backward loss (4.1)

and HSED uses gradient descent method to update the parameters $\theta_{f,j}$, $\theta_{b,j}$ for main state Center_j and minimize the loss for each state.

4.4 Reconstruction with Hybrid State

So far, HSED retrieves the encoding features $\operatorname{Embedding}_j(S_i)$ for each main state and KPI sensor S_i . For each KPI sensor S_i , we concatenate the feature $\operatorname{Embedding}_j(S_i)$ with the hybrid-state matrix and feed it in to a LSTM-based decoder to reconstruct the original sequence (See Algorithm 4). In this step, we update the parameter with gradient descent to minimize the following reconstruction loss:

Loss =
$$\sum_{i=1}^{n} \mathbf{P}_{i,j} \| S_i - S'_i \|_2^2 + \sum_{i=1}^{n} \mathbf{P}_{i,j} \| S_{i,b} - S'_{i,b} \|_2^2$$

Backward Reconstruction Error

4.5 Anomaly Detection

After training the model by four steps, HSED combines the stateaware models and detects the anomalies for online sequence X = [C, S]. Similar to the training process, the anomaly detection also consists of four steps. In the first step, HSED implies the deep temporal clustering method (Algorithm 2) with the state series C and generate the state-embedding vector Enc(C). Next, HSED uses the similarity matrix to compute the euclidean distance between Enc(C) and each main stateCenter_{*j*}, and discover the hybrid hidden states with Student's t distribution (Line 3 in Algorithm 1). In the third step, HSED encodes the KPI sensor S for each main state (Algorithm 2) and generates embedding features $\{\text{Embedding}_{i}(S)\}_{i=1}^{m}$. Finally, HSED reconstructs the original KPI sensor data S' and S'_h with hybrid hidden models (Algorithm 4). Based on the reconstruction error between the original series S and reconstructed data S', S'_{b} , HSED computes the reconstruction error as the anomaly score and report an alert if the anomaly score is higher than a threshold. In addition, HSED can also compute a confidence score based on the distribution of the hybrid hidden states.

5 PERFOMANCE EVALUATION

5.1 Experiment Setting

Engine dataset: This dataset contains 17 sensors collected from an IoT on vehicle engine and includes over 10000 timestamps. There are multiple work states of the eninge, and we focus on detect the following anomalies related to engine failure:

- High temperature: the engine temperature is too high.
- Misfiring: One or more engine cylinders are misfiring.
- Acceleration problem: Engine load has fluctuations or irregularities.

Compared method: We compare the HSED with the EncDec-AD method [9], which directly reconstruct the original time-series behavior with LSTM-Based auto-encoder.

For the engine dataset, we first use max-min operation to normalize each data and then divide the data-set to sliced window with length 150. After using the HSED algorithm, the average squurereconstructed error is 0.1348. In comparison, the reconstructed error of EncDec-AD is 0.1532, which has a worse performance than our novel method.

6 CONCLUSION

In this work, we proposed a new algorithm, called HSED, for IoT anomaly detection across various work state. HSED first introduce a state encoders to discover the hybrid model for the dynamic work state and later, employs a LSTM-based auto-encoder for reconstructing the original sensor signal. The evaluation on real-world datasets also suggests the superiority of HSED over state-of-the-art anomaly detection models.

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Figure 2: This Figure depicts the reconstruction sequence for the attribute "Calculated Engine Load". For the second KPI sensor, there exist a large deviation between the original sequence and the reconstructed sequence. Under this situation, it may be caused from acceleration problems and will report anomaly events to the agent.

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